#### CSC7426: Intro to Software & Data Engineering

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http://jpaulgibson.synology.me/~jpaulgibson/TSP/ Teaching/CSC7426/

### MinMaxAlgorithm

.../CSC7426/MinMaxAlgorithm.pdf

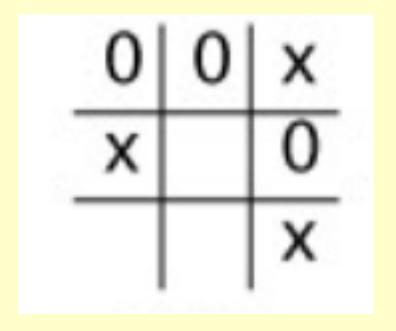
## Alpha-beta pruning: a classic algorithm in AI (arising from minmax theorem)

Von Neumann, John, and Oskar Morgenstern. "Theory of games and economic behavior." *Bull. Amer. Math. Soc* 51 (1945): 498-504.

Fuller, Samuel H., and John G. Gaschnig. "Analysis of the alphabeta pruning algorithm." (1973).

Knuth, Donald E., and Ronald W. Moore. "An analysis of alphabeta pruning." *Artificial intelligence* 6.4 (1976): 293-326.

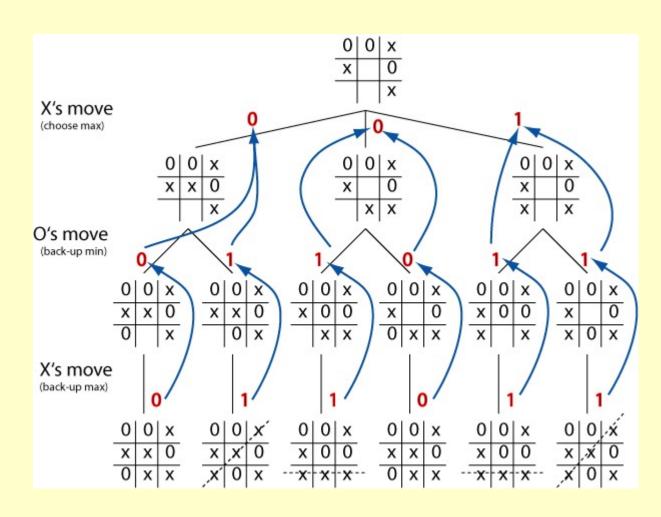
#### **Noughts and Crosses**



X to play - how could a machine/algorithm know that it should play the bottom-left in order to win?

# KR-IST - Lecture 5a Game playing with Minimax and Pruning, Chris Thornton

http://www.sussex.ac.uk/Users/christ//crs/kr-ist/lec05a.html



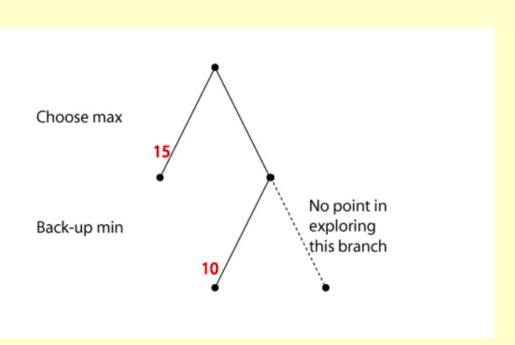
X win +1 Draw 0 O win -1

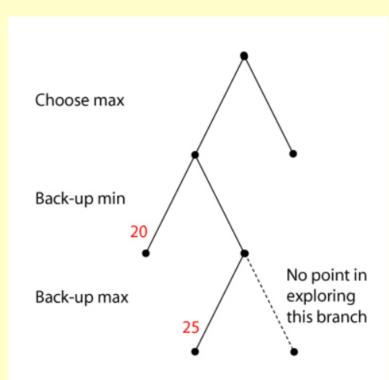
#### KR-IST - Lecture 5a Game playing with Minimax and

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http://www.sussex.ac.uk/Users/christ//crs/kr-ist/lec05a.html

#### Alpha-beta pruning





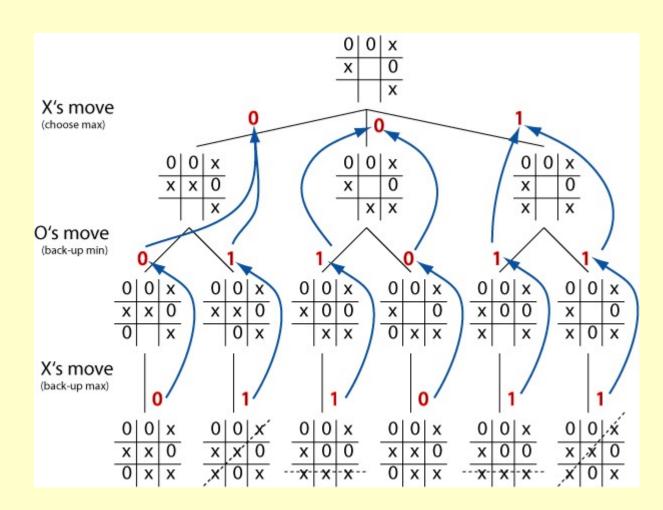
if (possible\_min < current\_max)
prune</pre>

if (possible\_max > current\_min)
prune

Alpha-cutoff

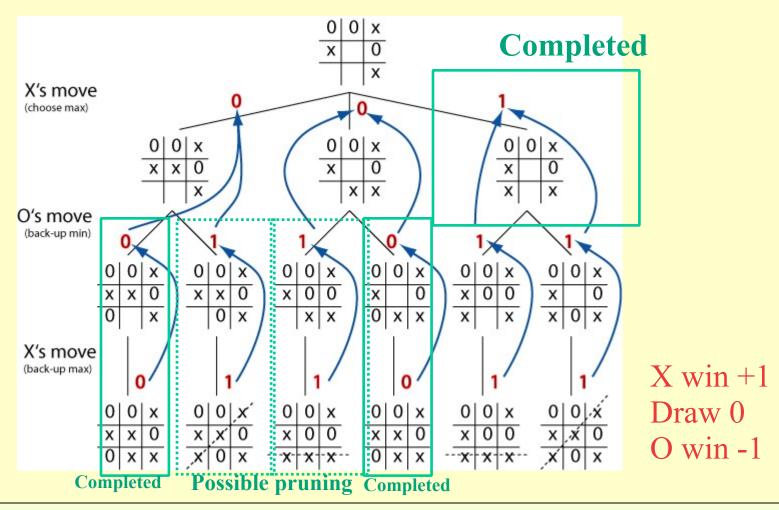
**Beta-cutoff** 

#### QUESTION: where could pruning be applied here?



X win +1 Draw 0 O win -1

#### **QUESTION:** where could pruning be applied here?



2023: J Paul Gibson CSC7426: MinMax Algorithm

#### Minmax pruning for perfect XO player

Implement a perfect XO player:

- 1) Using min-max without pruning
- 2) Using min-max with alpha-beta pruning
- 3) Compare the performance of the players against each other